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# Three-dimensional entanglement on a silicon chip

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Entanglement is a counterintuitive feature of quantum physics that is at the heart of quantum technology. High-dimensional quantum states offer unique advantages in various quantum information tasks. Integrated photonic chips have recently emerged as a leading platform for the generation, manipulation and detection of entangled photons. Here, we report a silicon photonic chip that uses interferometric resonance-enhanced photon-pair sources, spectral demultiplexers and high-dimensional reconfigurable circuitries to generate, manipulate and analyse path-entangled three-dimensional qutrit states. By minimizing on-chip electrical and thermal cross-talk, we obtain high-quality quantum interference with visibilities above 96.5% and a maximally entangled-qutrit state with a fidelity of 95.5%. We further explore the fundamental properties of entangled qutrits to test quantum nonlocality and contextuality, and to implement quantum simulations of graphs and high-precision optical phase measurements. Our work paves the path for the development of multiphoton high-dimensional quantum technologies.

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### **INTRODUCTION**

Entanglement is a central resource for quantum-enhanced technology, including quantum computation<sup>1</sup>, communication<sup>2</sup> and metrology<sup>3</sup>. To demonstrate the advantage of quantum systems, it is necessary to generate, manipulate and detect entangled states. Quantum states span the Hilbert space with a dimensionality of  $d^n$ , where d is the dimensionality of a single particle and n is the number of particles in the entangled states. Most of the widely used quantum information processing protocols are based on qubits, a quantum system with d = 2. Recently, higher-dimensional entangled states (qudits, d > 2) have gained substantial interest, owing to their distinguishing properties. For example, gudits provide larger channel capacity and better noise tolerance in quantum communication<sup>4–7</sup>, as well as higher efficiency and flexibility in quantum computing<sup>8,9</sup> and simulations<sup>10</sup>. From the fundamental point of view, qudits also provide stronger violations of Bell inequalities<sup>11</sup>, lower bounds for closing the fair-sampling loopholes in Bell tests<sup>12</sup> and possibilities to test contextuality<sup>13</sup>. Recent reviews on the high-dimensional entanglement can be found in refs <sup>14,15</sup>.

High-dimensional entangled photons have been realized in various degrees of freedom (DOFs), including orbital angular momentum (OAM)<sup>11,16</sup>, frequency<sup>17,18</sup>, path<sup>19,20</sup>, temporal<sup>21,22</sup> and hybrid time-frequency modes<sup>23</sup>. In particular, path-entangled photon pairs have been studied with a view to quantum information processing, where they are particularly attractive due to their conceptual simplicity<sup>24</sup>. However, the generation of high-dimensional path-entangled photon pairs typically requires the simultaneous operation of several coherently pumped indistinguishable photon-pair sources and several multi-path interferometers with high phase stability<sup>25</sup>. As the dimensionality increases, the phase stabilization quickly becomes a daunting task in experiments based on bulk and fibre optical elements.

Integrated photonic circuits based on silicon offer dense component integration, high optical nonlinearity and good phase stability, which are highly desirable properties for photonic quantum technology<sup>26–31</sup>. Moreover, silicon photonic devices are routinely fabricated in complementary metal oxide semiconductor (CMOS) processes. Therefore, a new field called silicon quantum photonics has recently been developed and has emerged as a promising platform for large-scale quantum information processing<sup>32</sup>. Recent advances of on-chip high-dimensional entanglement have employed frequency-encoding generated from a micro-resonator photon-pair source<sup>17</sup> and path-encoding generated from meander waveguides photon-pair source<sup>20</sup>. Specifically, silicon waveguides with cm-length are often employed as sources to create photon-pairs<sup>9,20,28</sup>. However, the natural bandwidth of the photons generated from meander waveguides is about 30 nm<sup>20</sup>. In order to obtain high-quality photons, it is necessary to employ bandpass filters (~1 nm bandwidth in ref. <sup>20</sup>), which unavoidably reduces the photon count rate drastically.

In this work, we employ a silicon photonic chip using an advanced resonator source embedded in Mach-Zehnder interferometers (MZIs) to generate, manipulate and characterize pathentangled gutrits (d = 3). Cavity-enhanced processes and independent tuning capabilities of the coupling coefficients of pump, signal and idler photons allow us to generate highindistinguishable and high-brightness photons without using passive filtering. The bandwidth of the photon generated from our source is about 50 pm, about a factor of 600 narrower to that of ref. <sup>20</sup>. This narrow-band feature not only provides high-quality single photons, but also holds the promise for direct coupling with telecom quantum memory<sup>33</sup>, which is not possible for the nanowire source due to the prohibitive low count rate after ~GHz bandwidth filtering. In particular, we perform the on-chip test of quantum contextuality with the closed compatible loophole. Furthermore, using the entangled-qutrit state, we simulate a two-vertex and three-edge graph and obtain the number of the perfect matchings of this graph, which is in the #Pcomplete complexity class<sup>34</sup>. Although the structure of the graph of our demonstration is simple, it can be viewed as the first step towards achieving the ambitious goal of solving #P hard problem

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with quantum photonic devices. We also employ our device to demonstrate the excellent phase sensitivity, exceeding both classical three-path linear interferometer and quantum second-order nonlinear interferometer limits. To be best of our knowledge, none of these three experiments have ever been realized with an integrated chip.

#### **RESULTS**

Silicon quantum photonic chip and experimental setup

We have employed a scalable scheme for generating high-dimensional entangled states<sup>25</sup>. As shown in the conceptual scheme (Fig. 1a), entangled qutrits are generated by three coherently pumped non-degenerate spontaneous four wave mixing (SFWM) photon-pair sources, in which two pump photons generate one signal photon and one idler photon with different wavelengths (Fig. 1b, c). The signal and idler photons are separated by dichroic mirrors (DMs) and then sent through reconfigurable linear optical circuits for implementing arbitrary 3-D unitary operations via three-dimensional multiports (3D-MPs). Finally, we verify and harness the qutrit entanglement by detecting single photons at the outputs.

To obtain an efficient photon-pair source, we use a dual Mach-Zehnder interferometer micro-ring (DMZI-R) photon-pair source<sup>35,36</sup>. Such a DMZI-R photon-pair source is inspired by the design of a wavelength division multiplexer (WDM) in classical optical communication<sup>37</sup> and could circumvent the trade-off between the utilization efficiency of the pump photon and the extraction efficiency of the signal and idler photon pairs from a ring resonator<sup>38</sup>. The DMZI-R photon-pair source was first demonstrated in ref. 35, where enhanced coincidence efficiency of a single source was shown. The working principle of the DMZI-R photon source is as follows: by wrapping two pulley waveguides around a ring resonator, one can construct a four-port device, as shown in Fig. 1b. We couple each waveguide at two points to the resonator, using four directional couplers. By adjusting the relative phases of two waveguides to the resonator, we can tune the coupling between waveguides to the resonator at the pump, signal and idler wavelengths independently. In the ideal case, we would like to have the pump circulate in the ring resonator to generate photon pairs, and therefore, the critical coupling condition for the pump is preferred. On the other hand, we want to extract the signal and idler photons from the resonator as soon as they are generated to minimize the propagation loss of photon pairs in the resonator. As a consequence, it is desirable to overcouple the waveguide to the resonator at the wavelengths of signal and idler photons. These two requirements can be fulfilled simultaneously by setting the free spectral range (FSR) of the MZIs to be twice that of the ring, such that every second resonance of the ring is effectively suppressed. By doing so, we can achieve the desired distinct coupling conditions for the pump, signal and idler photons and maximally utilize the pump to efficiently extract photon pairs. The ring has a radius of 15 µm and a coupling gap of 250 µm (200 µm) at the input (output) side. The length difference of the unbalanced MZI1 (MZI2) is 47.8 µm (48 µm). Optical microscopy images of the DMZI-R photon-pair source and the whole entangled-qutrit chip are shown in Fig. 1d, e, respectively. Note that the sizes of the gaps of critical and over-critical couplings depend on the propagating loss of the photons in the ring. One should be able to obtain a higher count rate by optimizing the gap size<sup>35</sup> (see Supplementary Information for a theoretical analysis and a detailed characterization of the DMZI-R photon source).

Following the DMZI-R photon-pair source, we use an asymmetric MZI (AMZI) as an on-chip WDM to separate the non-degenerate signal and idler photons. As shown in Fig. 1f, we repeat this combination of DMZI-R source and WDM three times,

and excite these sources coherently. When the generation rate is the same for all three sources and the relative phases of the pump are all zero, we generate a maximally entangled state of two qutrits:  $|\Psi\rangle = \frac{1}{\sqrt{3}}(|00\rangle + |11\rangle + |22\rangle)$ . Note that  $|0\rangle$ ,  $|1\rangle$  and  $|2\rangle$  are the individual path states of single photons.

Each gutrit can be locally manipulated by a 3D-MP<sup>24</sup>, which is composed of thermo-optic phase shifters (PSs) and multi-mode interferometers (MMIs). In particular, one of the essential components, formed by a single PS and a tunable beam splitter, is realized with a MZI, consisting of two balanced MMIs and a PS. These components are used to realize  $R_z(\varphi_z)$  and  $R_v(\theta_v)$  rotations, and thus to obtain an arbitrary SU(2) operation in the twodimensional subspace. Note that our experimental configuration is also closely related to a recent proposal on generating OAM entanglement by path identity<sup>39</sup>. The collective paths and individual paths in our work correspond to the path and OAM in ref. <sup>40</sup>. After manipulating and characterizing the entangled gutrits with two 3D-MPs, both the signal and idler photons are coupled out from the chip, filtered to suppress residual pumping with off-chip filters, and detected with superconducting nanowire single-photon detectors (SSPDs). The single-photon detection events are recorded by a field-programmable gate array (FPGA)based timetag unit. Then both single counts and coincidence counts  $CC_{ij}$  between path i (i = 1, 3, 5) and path j (j = 2, 4, 6) are extracted from these timetag records (see Supplementary Information for further experimental details).

#### From qubit entanglement to qutrit entanglement

To generate three-dimensional (3D) path-entangled photons, it is necessary to ensure that all three coherently pumped photon-pair sources are identical. This means that the emitted photon pairs from different sources should be the same in all DOFs, including polarization, spatial mode, count rate and frequency. For our chipbased system, we use single-mode waveguides, which automatically give us the same polarization states and spatial modes of photons from different sources. However, the count rate and frequency of the photons are not necessarily identical for different sources. To eliminate the count rate distinguishability, we can tune the pump power of the individual source. The last DOF is the frequency. In non-resonant broad band (~nm to tens of nm) photon-pair sources, such as silicon nanowires, one can use offchip narrow-band filtering to post-select identical spectra of different photons<sup>9,20</sup>, which unavoidably reduces the count rate. In the resonant sources, such as our DMZI-R source, we can actively tune the resonance wavelengths of each individual source with PSs. In doing so, we obtain identical photons without sacrificing the photon count rate, which is particularly important for multiphoton high-dimensional experiments. However, aligning the frequency of the narrow-band photons generated from resonance-enhanced sources is challenging within the sub-mm foot-print of our chip. The reasons are follows: silicon has a relatively high thermo-optic coefficient. On the one hand, this feature of silicon is desirable for realizing reconfigurable photonic circuits by using thermo-optic PSs with low power consumption. On the other hand, it presents an experimental challenge to stabilize the frequency of the single photons generated from resonance-enhanced photon-pair sources under several distinct configurations of thermal PSs, due to thermal cross-talk<sup>41</sup>.

As the first step to generate 3D entanglement, we verify the identicality of two sources with time-reversed Hong-Ou-Mandel (RHOM) interference<sup>42</sup>. Highly indistinguishable photons produce the high visibility of RHOM interference. We investigate the indistinguishability between all pairs of the three sources by interfering signal-idler photon pairs generated from S1, S2 and S3 on the top 3D-MP. For instance, we set the phases  $S_{y1}$  and  $S_{y2}$  to be  $\pi$  and  $S_{y3}$  to be  $\pi/2$  and scan the phase of  $S_{z3}$  to obtain the RHOM interference fringe between S2 and S3. The RHOM

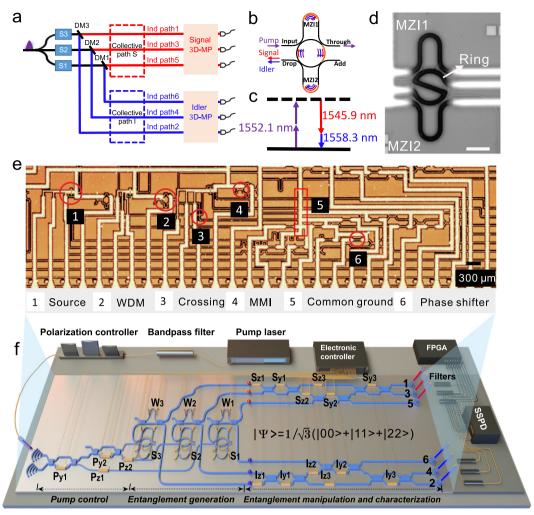


Fig. 1 Silicon quantum photonic chip and schematic of the experimental setup. a Conceptual scheme of the approach for generating and manipulating two entangled qutrits. Three non-degenerate photon-pair sources, S1, S2 and S3, are coherently pumped, and three dichroic mirrors, DM1, DM2 and DM3, separate signal and idler photons into two collective paths S and I, which consist of three individual (Ind) paths 1, 3 and 5, and 2, 4 and 6, respectively. Then two three-dimensional multiport interferometers (3D-MP) perform unitary transformations to the entangled qutrits. b Diagram of a dual Mach-Zehnder interferometer micro-ring (DMZI-R) photon-pair source. This source has four ports: input, throughput, add and drop. Pump photons are sent into the input port and critically coupled into the ring resonator, where signal and idler photons are generated. By adjusting the phases of MZIs 1 and 2, we can reduce the photon leakage into the through port and increase the signal and idler photons coupling to the drop port. c Two identical pump photons (1552.1 nm) generate one signal (1545.9 nm) and one idler (1558.3 nm) photons in non-degenerate spontaneous four wave mixing, d Optical microscopy image of the DMZI-R photon-pair source, with scale bar representing 20 µm. Thermo-optical phase shifters (PSs) are shown as thick black curves. e Optical microscopy image of the whole entangled gutrit chip. Several important on-chip elements are labelled: (1) DMZI-R photon-pair source; (2) wavelength division multiplexer (WDM); (3) crossing; (4) multi-mode interferometer (MMI); (5) common ground of the electrical signals; (6) thermo-optic PS. f Schematic of the complete experimental setup. A picosecond pump pulse is filtered, polarized and coupled into the chip via a bandpass filter, a polarization controller and a grating coupler, respectively. A photon pair is created in a superposition between three coherently pumped DMZI-R sources (S1-3). By adjusting four PSs for the pump ( $P_{y1}$ ,  $P_{y2}$ ,  $P_{z1}$  and  $P_{z2}$ ), we can generate a tunable qutrit entangled state. The signal (red) and idler (blue) photons are separated by W1-3 and routed to two 3D-MPs, which are composed of 12 MMIs and 12 PSs and enable us to implement arbitrary 3D local unitary transformation. Both signal and idler photons are then coupled out from the chip, filtered and detected by six grating couplers, filters and superconducting single-photon detectors (SSPDs). Coincidence events are recorded by an FPGA-based timetag unit. All on-chip PSs are controlled with current sources.

interference fringes between S1 and S2, S1 and S3 and S2 and S3 are shown in Fig. 2a–c, respectively. The visibility of the fringe is defined as  $V=(CC_{max}-CC_{min})/(CC_{max}+CC_{min})$ , where  $CC_{max}$  and  $CC_{min}$  are the maximum and minimum of the coincidence counts. The measured visibilities are greater than 96.49% in all cases, indicating high-quality spectral overlaps. All of our data are raw, and no background counts are subtracted. To obtain high interference visibilities, we have spent significant amount of efforts to eliminate thermal noise (see Supplementary Information for further experimental details). We believe that by using better designs of the thermal PSs such as reported in refs  $^{43,44}$ , the noise

can be greatly mitigated. In additional to reduce cross-talks, for reaching a visibility required for the practical applications, high-fidelity quantum control is a necessity. Remarkably, previous work has shown one can achieve excellent on/off ratio (~0.5 dB), equivalent to having a Pauli-Z error rate of  $<10^{-6.45}$  by using cascaded MZIs. Over 100 dB pass-band to stop-band contrast filters have also been realized by cascaded microrings<sup>46</sup> and AMZIs<sup>47</sup>, respectively. By combining these high-performance devices, we believe integrated quantum photonics is a promising route in the development of future quantum technologies and applications<sup>48</sup>.

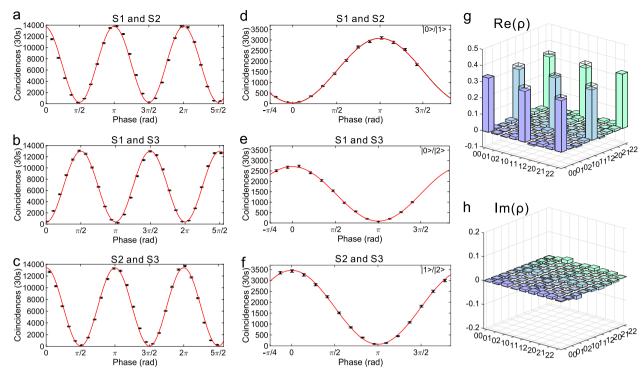


Fig. 2 Quantum interference and entanglement of two qutrits. Interference fringes of the two-photon RHOM experiments are shown in  $\mathbf{a}$ -c for S1 and S2, S1 and S3 and S2 and S3, respectively. The measured visibilities are greater than 96.49% in all three cases, indicating high-quality indistinguishabilities between the three sources. Path-correlations of the three two-qubit subspaces for the entangled-qutrit state  $\frac{1}{\sqrt{3}}(|00\rangle+|11\rangle+|22\rangle)$  are shown in  $\mathbf{d}$ - $\mathbf{f}$  for S1 and S2, S1 and S3, and S2 and S3, respectively. The signal photon is projected on to  $\frac{1}{\sqrt{2}}(|j\rangle+|k\rangle)$ , and the idler photon is measured in the base  $\frac{1}{\sqrt{2}}(|j\rangle+e^{i\varphi}|k\rangle)$  with  $\varphi$  being the scanning phase and with (j,k)=(0,1), (0,2) and (1,2), respectively. The measured visibilities are greater than 94.72% in all three cases, indicating high-quality path entanglement. The points are experimental data, and the curves are fits. The uncertainties denote the standard deviations from the Poisson distribution of the raw photon counts. The real and imaginary parts of the reconstructed density matrix of the two-photon entangled-qutrit state are shown in  $\mathbf{g}$  and  $\mathbf{h}$ . Eighty-one measurement settings are decomposed into  $|p_s\rangle\otimes|p_i\rangle$ , where  $|p_k\rangle=|\psi_k\rangle\langle\psi_k|$ .  $|\psi_k\rangle$  is chosen from the following set:  $|0\rangle$ ,  $|1\rangle$ ,  $|2\rangle$ ,  $|1\rangle$ ,  $|2\rangle$ ,  $|1\rangle$ 

The next step is to verify the qubit entanglement of path states between three different pairs of sources. We measure the correlation of the path-entangled states in mutually unbiased bases (MUBs). We set the measurement base of the signal photon to be the coherent superpositions of the computational base,  $\frac{1}{\sqrt{2}}(|j\rangle + |k\rangle)$ , where (j,k) = (0,1), (0,2), (1,2). Then, we scan the phase  $\varphi$  in the quantum state of the idler photon,  $\frac{1}{\sqrt{2}}(|j\rangle + e^{i\varphi}|k\rangle)$ and measure the coincidence counts between the signal and idler photons. The coincidence fringes are shown in Fig. 2d-f for S1 and S2, S1 and S3 and S2 and S3, respectively. The values of various visibilities range from  $94.72\% \pm 0.50\%$  to  $97.50\% \pm 0.38\%$ , indicating high-quality gubit entanglement. The phase doubling signature of RHOM fringes compared to the correlation counterparts can be seen by comparing Fig. 2a-c, and Fig. 2d-f. In the RHOM experiment, both signal and idler photons create a coherent superposition of two photons in two paths, the state that evolves under a phase shift in one of the modes then displays the phase doubling<sup>42</sup>. Note that the count rate of the pathcorrelation measurement is lower than that of the RHOM measurement, mainly because the design of the on-chip WDM is not optimal. Higher count rates of the correlation measurement can be achieved by optimizing the length difference between the two arms of the WDM.

Having established high-quality qubit entanglement, we proceed to characterize the qutrit entangled state with complete

high-dimensional quantum-state tomography (QST). We use a set of all possible combinations of Gell-Mann matrices and apply the corresponding settings to both 3D-MPs<sup>49</sup>. The QST method takes approximately 33 mins with a typical count rate ~100 Hz per setting. Figure 2g, h displays the real and imaginary parts of the reconstructed density matrix of the state, respectively, showing good agreement between the maximally entangled and measured quantum states with a fidelity of  $95.50\% \pm 0.17\%$ . The maximum matrix element of the imaginary part is smaller than 0.015. From the reconstructed density matrix, we obtain an Iconcurrence of  $1.149 \pm 0.002^{50}$ . The uncertainties in the state fidelity extracted from these density matrices are calculated using a Monte Carlo routine assuming Poissonian statistics. In the context of quantum communication, a multi-dimension entanglement-based Ekert91 QKD protocol51 was initially proposed and analyzed in refs 52,53, where high-dimension mutually unbiased bases correlations between two Alice and Bob can be used to generate keys. The upper bound error rate (ER) that guarantees security against coherent attacks for device-dependent QKD in three dimensions is 15.95%. For a maximally gutrit entangled state, the fidelity (F) of the state can be used to infer the ER if Alice and Bob use the same MUB<sup>54</sup>; that is F = (3-4\*ER)/3. From the fidelity we obtain, the ER is only 3.375%, which is considerably below the required bound, indicating the high quality of our qutrit state.

Tests of quantum nonlocality and contextuality with entangled qutrits

To benchmark the high-quality qutrit entanglement and high-precision quantum control, we demonstrate experimental tests of quantum nonlocality and quantum contextuality. Violations of Bell inequalities based on local realistic theories provide evidence of quantum nonlocality. It has been demonstrated that, high-dimensional correlations compatible with local realism satisfy a generalized Bell-type inequality, the Collins-Gisin-Linden-Massar-Popescu (CGLMP) inequality, with  $I_d \le 2$  for all  $d \ge 2^{55}$ . Expression  $I_3$  is given by joint probabilities as

$$I_{3} = [P(A_{1} = B_{1}) + P(B_{1} = A_{2} + 1) + P(A_{2} = B_{2}) + P(A_{1} = B_{2})] - [P(A_{1} = B_{1} - 1) + P(B_{1} = A_{2}) + P(A_{2} = B_{2} - 1) + P(B_{2} = A_{1} - 1)],$$
(1)

where  $P(A_a = B_b + k)$  with (a, b = 1, 2) and (k = 0, 1) represent the joint probabilities for the outcomes of  $A_a$  that differ from  $B_b$  by k. The measurement bases used to maximise the violation of Eq. (1) for the maximally entangled state  $|\Psi\rangle = \sum_{j=0}^2 |j\rangle_A \bigotimes |j\rangle_B$  are defined as

$$|K\rangle_{A,a} = \frac{1}{\sqrt{3}} \sum_{j=0}^{2} \exp\left[i\frac{2\pi}{3}j(K+\alpha_a)\right]|j\rangle_A,$$
 (2)

$$|L\rangle_{B,b} = \frac{1}{\sqrt{3}} \sum_{i=0}^{2} \exp\left[i\frac{2\pi}{3}j(-L + \beta_b)\right]|j\rangle_{B},\tag{3}$$

where  $i = \sqrt{-1}$ ,  $\alpha_1 = 0$ ,  $\alpha_2 = 1/2$ ,  $\beta_1 = 1/4$  and  $\beta_2 = -1/4$ , K and L ∈ {0, 1, 2} denote Alice's and Bob's measurement outcomes respectively, and  $|i\rangle$  denotes the computational basis. These measurement bases can be implemented by configuring PSs in the 3D-MPs. For instance, we set  $S_{z1}=0.333\pi$ ,  $S_{y1}=0.5\pi$ ,  $S_{z2}=0.583\pi$ ,  $S_{y2}=0.392\pi$ ,  $S_{z3}=0.779\pi$  and  $S_{y3}=0.5\pi$  to realize setting A<sub>1</sub>. In the context of quantum computation, entanglement is the essential resource. For one-way quantum computation, ref. 23 reported the noise sensitivity of a two-photon, three-level and four-partite (two DOFs) cluster state with entanglement witness. CGLMP inequality is an entanglement criterion with higher correlation requirements comparing to entanglement witness. We witness the existence of entanglement between two gutrits in our experiment by using CGLMP inequality. The classical bound is violated by  $51.46\sigma$  ( $I_3 = 2.7307 \pm 0.0142$ ), benchmarking the resilience to errors. The experimental results for the four base settings are shown in Table 1.

Contextuality is a fundamental concept in quantum mechanics<sup>13,56–58</sup> and an important resource for fault-tolerant universal quantum computation<sup>59</sup>. A single qutrit is the simplest quantum system showing the contradiction between noncontextual hidden-variable models and quantum mechanics<sup>13</sup>. However, the testability of the Kochen-Specker (KS) theorem is debated due to the finite precision in a single qutrit in practical experiments<sup>60,61</sup>. An approach based on maximally entangled-qutrit pair has been proposed<sup>62</sup>, which was recently realized with bulk optics<sup>63</sup>.

The experimental setting is as follows. A pair of maximally entangled qutrits is sent to two parties, Alice (A) and Bob (B). Alice performs projective measurements, either  $D_1^A$  or  $T_0^A$ ,  $T_1^A$ , and Bob simultaneously performs measurement  $D_0^B$ , where  $D_1^A$  and  $D_0^B$  are dichotomic projectors with two possible outcomes, 0 or 1, and  $T_0^A$  and  $T_1^A$  are trichotomic projectors with three possible outcomes, a, b or c. These four projectors are defined as  $D_0^B = |i\rangle\langle i|$ ,  $D_1^A = |f\rangle\langle f|$ ,  $T_0^A = |a_0\rangle\langle a_0|$  and  $T_1^A = |a_1\rangle\langle a_1|$ , where  $|i\rangle = (|0\rangle + |1\rangle + |2\rangle)/\sqrt{3}$ ,  $|f\rangle = (|0\rangle - |1\rangle + |2\rangle)/\sqrt{3}$ ,  $|a_0\rangle = (|1\rangle - |2\rangle)/\sqrt{2}$  and  $|a_1\rangle = (|0\rangle - |1\rangle)/\sqrt{2}$ . The non-compatibility loophole

contextuality inequality can be expressed as<sup>62</sup>:

$$P(D_1^A = 1|D_0^B = 1) - P(T_0^A = 1|D_0^B = 1) - P(T_1^A = 1|D_0^B = 1) \le 0,$$
(4)

where  $P(D_1^A=1|D_0^B=1)$  stands for the conditional probability of Alice obtaining result 1 for  $D_1^A$  when Bob also obtains result 1 with  $D_0^B$ .  $P(T_0^A=1|D_0^B=1)$  and  $P(T_1^A=1|D_0^B=1)$  are defined analogously. For our experiment, we need to reconfigure two 3D-MPs according to these projectors and measure the coincidence counts to reconstruct the conditional probabilities in Eq. (4). For example,  $|f\rangle$  can be projected to port 3 by setting  $S_{z1}=0$ ,  $S_{y1}=0.5\pi$ ,  $S_{z2}=1.25\pi$ ,  $S_{y2}=0.608\pi$ ,  $S_{z3}=0$  and  $S_{y3}=\pi$ . We experimentally violate the noncontextuality inequality by 9.5 standard deviations (0.085  $\pm$  0.009). The detailed experimental results are listed in Table 2. The no-signaling conditions, confirming the compatibility assumption between the measurements of Alice and Bob, are checked, as shown in Table 3. The results deviate slightly from 0 because of experimental imperfections.

Harnessing two-qutrit quantum correlations: quantum simulation of graphs and quantum metrology

High-order quantum correlations are unique properties of high-dimensional entangled quantum systems and are a central resource for quantum information processing. To probe the quantum correlations in the entangled-qutrit system, we measure the coincidence counts between the signal and idler photons under different MUBs by tuning both the phases of the signal/idler and pump photons. Here we use the quantum correlation between two entangled qutrits to demonstrate the quantum simulation of graphs and quantum metrology based on a quantum multi-path interferometer with third-order nonlinearity.

Quantum simulation of graphs. Graphs are mathematical structures for describing relations between objects and have been widely used in various areas, including physics, biology and information science. A graph typically consists of a set of vertices and edges connecting the vertices. A subset of the edges containing every vertex of the n-vertex graph exactly once is defined as a perfect matching of the graph. To find the number of perfect matchings of a graph is a problem that lies in the #P-complete complexity class<sup>34</sup>. To provide an algorithm to solve

**Table 1.** Detailed experimental results leading to a violation of the CGLMP inequality.

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Probability	Result	Expected value
$P(A_1 = B_1)$	0.7664 ± 0.0059	0.8293
$P(A_1 = B_1 - 1)$	$0.1480 \pm 0.0050$	0.1111
$P(A_1 = B_2)$	$0.8098 \pm 0.0054$	0.8293
$P(A_1 = B_2 + 1)$	$0.1030 \pm 0.0042$	0.1111
$P(A_2 = B_1 - 1)$	$0.8292 \pm 0.0052$	0.8293
$P(A_2 = B_1)$	$0.1014 \pm 0.0041$	0.1111
$P(A_2 = B_2)$	$0.8011 \pm 0.0055$	0.8293
$P(A_2 = B_2 - 1)$	$0.1233 \pm 0.0045$	0.1111

**Table 2.** Detailed experimental results for the test of the noncontextuality inequalities.

Conditional probability	Result	Expected value
$P(D_1^A = 1   D_0^B = 1)$	$0.1245 \pm 0.0080$	0.111
$P(T_0^A = 1 D_0^B = 1)$	$0.0253 \pm 0.0035$	0
$P(T_1^A = 1 D_0^B = 1)$	$0.0136 \pm 0.0027$	0

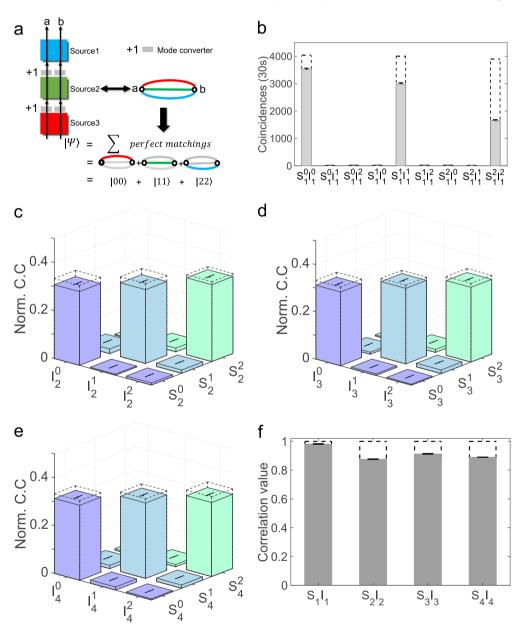


such a hard problem is highly desirable. Recent studies have shown that a carefully designed quantum optical experiment can be associated with an undirected graph<sup>64</sup>. In Particular, the number of coherently superimposed terms of the generated high-dimensional quantum state from a quantum optical experiment is

Table 3. No-signaling results between Alice and Bob	
Probability	Result
$\begin{aligned} &   P(D_0^B = 1   D_1^A, D_0^B) - P(D_0^B = 1   T_0^A, D_0^B)   \\ &   P(D_0^B = 1   D_1^A, D_0^B) - P(D_0^B = 1   T_1^A, D_0^B)   \\ &   P(D_0^B = 1   T_0^A, D_0^B) - P(D_0^B = 1   T_1^A, D_0^B)   \end{aligned}$	0.0236 ± 0.0089
$ P(D_0^B = 1 D_1^A, D_0^B) - P(D_0^B = 1 T_1^A, D_0^B) $	$0.0094 \pm 0.0088$
$ P(D_0^B = 1 T_0^A, D_0^B) - P(D_0^B = 1 T_1^A, D_0^B) $	$0.0330 \pm 0.0087$

exactly the number of perfect matchings in the corresponding graph. Each vertex stands for an optical path occupied by a single photon and every edge represents a photon-pair source. This scheme can be viewed as a quantum simulation of graphs.

As the first step towards the quantum simulation of graphs, we use entangled qutrits to experimentally demonstrate the connection between graph theory and quantum optical experiments. Figure 3a shows a conceptual scheme of our realization. Each pair of photons generated from sources propagates along their paths, denoted by black arrows, and acquires additional mode shifts due to the mode converters between the sources. As mentioned above, the path and OAM in ref. <sup>64</sup> are equivalent to the collective and the individual paths of our integrated quantum photonic circuit, as shown in Fig. 1a. Therefore, the



**Fig. 3 Quantum simulation of graphs. a** The optical setup corresponding to the experimental implementation on the chip and the corresponding graph. A two-fold coincidence in the experiment can be seen as a subset of edges containing each of the vertices only once, which is called a perfect matching in the graph. A coherent superposition of three perfect matchings leads therefore to the quantum state  $|\Psi\rangle=\frac{1}{\sqrt{3}}(|00\rangle+|11\rangle+|22\rangle$ . **b** The measured coincidence counts between the signal and idler photons on the computational basis,  $S_1I_1$ . Dashed empty bars are deduced results by balancing the loss for every port. **c-e** The balanced normalized coincidence results for  $S_2I_2$ ,  $S_3I_3$  and  $S_4I_4$ . **f** The experimental correlation coefficients are measured in all four MUBs  $(S_1I_1, S_2I_2, S_3I_3 \text{ and } S_4I_4)$  for the entangled qutrits. Ideal results are shown with dashed empty bars. The uncertainties denote the standard deviations from the Poisson distribution for raw photon counts.

mode converters can be implemented by routing the individual paths of the photon on our chip. By suitably setting up the 3D-MPs, we verify the resultant quantum state with coherent superimposed terms corresponding to the number of perfect matchings. We implement two experimental steps to realize this goal. First, we measure the coincidence counts between the signal and idler photons on the computational basis,  $S_1I_1$ . The experimental results are shown in Fig. 3b. It is clear that the major contributions are the 00, 11 and 22 terms. The second step is to verify the coherence between these three terms. For the entangled-qutrit pair system, each individual qutrit has four MUBs. Therefore, we have to measure the correlation coefficients in all four base combinations, i.e.  $S_1I_1$ ,  $S_2I_2$ ,  $S_3I_3$  and  $S_4I_4$ , where  $S_k = I_k^*$ , with (k = 1, 2, 3, 4). These MUBs, up to normalization, are defined as

$$S_{1} = (1,0,0), (0,1,0), (0,0,1),$$

$$S_{2} = (1,1,1), (1,\omega,\omega^{*}), (1,\omega^{*},\omega),$$

$$S_{3} = (1,\omega,1), (1,\omega^{*},\omega^{*}), (1,1,\omega),$$

$$S_{4} = (1,\omega^{*},1), (1,1,\omega^{*}), (1,\omega,\omega),$$
(5)

where  $\omega = e^{i\frac{2\pi}{3}}$  and \* stands for the complex conjugation.

The normalized coincidence counts of  $S_2I_2$ ,  $S_3I_3$  and  $S_4I_4$  are shown in Fig. 3c–e, respectively, by balancing the loss for every port. The experimental correlation coefficients derived from the coincidence counts in the four MUB combinations are shown in Fig. 3f. For an ideal maximally entangled-qutrit pair, the correlation coefficients should be unity. Due to the experimental imperfections, we obtain the correlation coefficients with the values of  $98.17\% \pm 0.11\%$ ,  $87.61\% \pm 0.27\%$ ,  $91.32\% \pm 0.24\%$  and  $89.01 \pm 0.27\%$ , which shows correlations in all MUBs.

Quantum metrology with entangled qutrits. Accurate phase measurements are at the heart of metrological science. One figure-of-merit for evaluating the accuracy of phase measurement is sensitivity, S, which is defined as the derivative of the output photon number with respect to a phase change  $S \propto 1/N$ . In the experimental setting of classical interferometers, it is well known that increasing the number of paths of the interferometer can enhance the sensitivity<sup>65</sup>. On the other hand, in the field of quantum metrology, one can further enhance the sensitivity by using entanglement<sup>3</sup>. Here, we combine both traits from classical and quantum systems and employ a three-dimensionentanglement third-order-nonlinearity interferometer to demonstrate the enhanced phase sensitivity compared to the classical three-path<sup>66</sup> and quantum second-order-nonlinearity interferomsend the entangled-qutrit state We  $\frac{1}{\sqrt{3}}(e^{i2Pz1}|00\rangle + e^{i2Pz2}|11\rangle + |22\rangle$  into two separate 3D-MPs. We then scan the relative pump phases Pz1 and Pz2 and measure the coincidence between two qutrits (outputs 1,3,5 and 2,4,6). In total, there are nine different coincidence combinations. We quantify the autrit-autrit correlations as functions of phase settings of Pz1. Pz2. The normalized coincidences along with the theoretical results are shown in Fig. 4a-c. It is easily understood that the phase dependence is different between the second and thirdorder nonlinear interactions<sup>67</sup>. In the generation of entangled photon pairs, two pump photons are involved in the third-order processes providing a double phase compared to the secondorder processes with the participation of only one pump photon. The measurements confirm this difference. Specifically, if the phases are chosen such that Pz1 = -Pz2, the intensity varies from maximum to minimum as the pump phase is changed. This phase setting also gives the maximal sensitivity S. The raw data are

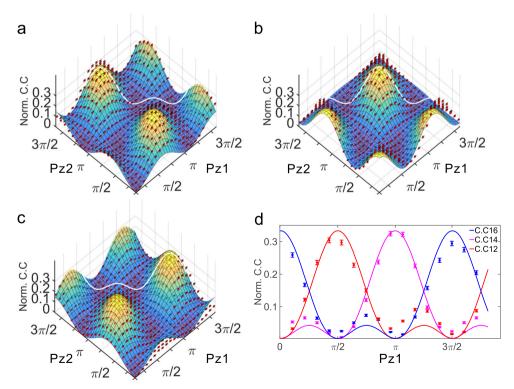


Fig. 4 Quantum metrology with the entangled qutrits state  $|\Psi\rangle=\frac{1}{\sqrt{3}}(e^{i2Pz1}|00\rangle+e^{i2Pz2}|11\rangle+|22\rangle)$ . **a–c** correspond to coincidence detection combinations of detectors (1,2) (1,4) and (1,6), respectively, with two relative pump phases Pz1 and Pz2 scanned. The normalized measured coincidences (Norm. C. C) (red dots) and simulated results without any free parameters (lines and surfaces) are shown. The data display excellent agreement with the theoretical predictions. **d** Diagonal cuts through the three-dimensional plots by setting Pz1 = -Pz2 in **a–c** reveal the typical structure of the three-path interferometer with a sensitivity of 1.476 ± 0.048, exceeding both classical three-path linear interferometer and quantum second-order nonlinear limits. The red, pink and blue points represent the experimental data extracted from **a–c** and are identified as white lines respectively. The curves show the theoretical results. The error bars are calculated by a Poissonian distribution.



extracted from the measured results and fitted with theoretical curves as shown in Fig. 4d. The averaged phase sensitivity  $S=\frac{1}{CC_{abmax}}|\frac{dCC_{ab}}{d\phi}|$  is  $1.476\pm0.048~{\rm rad}^{-1}$ , more than the theoretical ideal value of  $0.5~{\rm rad}^{-1}$  for the two-path interferometer and  $0.78~{\rm rad}^{-1}$  for the ideal three-path interferometer. The reason for the increased sensitivity is that the doubled phase sensitivity of the SFWM process and the side lobes appears between the two main peaks in three-path interference patterns, which enhance the steepness of the peaks of the correlations.

#### DISCUSSION

We have integrated three resonance-enhanced photon-pair sources embedded in interferometers, three WDMs and two 3D-MPs on a single monolithic silicon chip. We made all three sources identical without using frequency post-selection and observe high-visibility quantum interference, which allowed us to prepare, manipulate and analyse the high-quality path-entangled-qutrit state. We violated the CGLMP inequality to confirm quantum nonlocality and the KS inequality to confirm contextuality with the entangled qutrits, verifying fundamental properties of quantum theory. Furthermore, we used two-qutrit quantum correlations to simulate graphs and identify the number of perfect matchings for a small-scale graph. Finally, by using our chip for 3D entanglement, a third-order nonlinearity interferometer, we improved the phase sensitivity by a factor of 2 compared to a classical three-path interferometer.

Our demonstration of finding the number of the perfect matchings of the graph could be further extended to the multiphoton and higher-dimension experiments, which might be suitable to demonstrate the quantum advantage in the near or mid term. To reach this regime, one needs to develop high-brightness multiphoton sources. The source presented in this work is a promising candidate for such a source. Although there exist a few technical challenges towards full integrated silicon quantum chips, such as cryogenic-compatible photon manipulation and high-efficiency photon detection, heterogeneous integrated chips are a promising approach for achieving this goal 68-70. Combined with an efficient on-chip SSPD<sup>69</sup> and recently demonstrated cryogenic operation of Si-barium titanate<sup>70</sup>, our work could be viewed as a solid basis of future photonic quantum devices and systems for quantum information processing.

## **DATA AVAILABILITY**

The data that support the plots within this paper and other findings of this study are available from the corresponding author upon reasonable request.

#### **CODE AVAILABILITY**

The codes that support the plots within this paper and other findings of this study are available from the corresponding author upon reasonable request.

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#### **AUTHOR CONTRIBUTIONS**

L.L., L.X., Z.C. and X.M. designed and performed the experiment. L.C., T.Y., T.T., Y.P. and X.C. provided experimental assistance and suggestions. W.M. provided theoretical assistance. L.L., L.X. and X.M. analysed the data. L.L. and X.M. wrote the manuscript with input from all authors. Y.L., S.Z. and X.M. supervised the project. L.L, L.X. and Z.C. contributed equally to this work.

#### **COMPETING INTERESTS**

The authors declare no competing interests.

#### **ADDITIONAL INFORMATION**

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